



Fuzzy Data Mining and Fuzzy Reasoning

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ABSTRACT

In this paper, logical data independence for physical data independence for data mining is discussed. The fuzzy databases are studied for data mining with logical and physical data independence. Searching and statistical quantification with fuzzy logic is studied for fuzzy data mining. The fuzzy reasoning for data mining is discussed. The SQL queries are studied for fuzzy data mining.

Keywords

Fuzzy logic, fuzzy reasoning, data mining, fuzzy data mining, SQL

1. INTRODUCTION

The knowledge discovery with data mining necessary to improve business and reduce the cost of business. The data warehousing is necessary for data mining. The information stored in data warehousing may be data or text. The logical and physical data independence are required during join or decomposition of databases. Logical independence is most important before going to physical independence. Various query languages used to mining the information with data or text like SQL, QUEL and Xquery with warehousing. The data mining goal is search and statistical measures an algorithm running on data mining is scalable. It is continuum of analysis and exploration of data or text.

The data mining has different models like frequent item sets, associations, clustering and classification. It is great difficulty data mining with data warehousing for statistical analysis. The fuzzy databases will minimize the statistical analysis during online analytic process (OLAP) or online transaction process (OLTP). The fuzzy data mining methods can be defined using with SQL, QUEL and r Query.

In the following, the logical and phys data independence is studied for data mining by taking relational databases. The logical and physical data independence is studied for fuzzy data mining. The fuzzy reasoning is studied for data mining. The SQL query examples are given for data mining and fuzzy data mining. The fuzzy databases are studied with rough sets

2. RELATIONAL DATABASE

The relational database is defined as Cartesian product of Domains A_1, A_2, \dots, A_m and is represented as

$$R = A_1 \times A_2 \times \dots \times A_m$$

$t_i = a_{i1} a_{i2} \dots, a_{aim}, i = 1, \dots, n$ are tuples

or

$R(A_1, A_2, \dots, A_n)$, R is relation, A_1, A_2, \dots, A_m are domains

$R(a_{i1}, a_{i2}, \dots, a_{im}, i = 1, \dots, n$ are tuples

For instance,

| Cno | Ino | Iname | price |
|------|------|--------|-------|
| C101 | I105 | coffee | 100 |
| C101 | I107 | Milk | 50 |
| C103 | I104 | tea | 80 |
| C102 | I107 | milk | 80 |
| C101 | I108 | Sugar | 60 |
| C102 | I105 | coffee | 100 |

consider Price relational database

| ino | Iname | price |
|------|--------|-------|
| I105 | Coffee | 100 |
| I107 | Milk | 50 |
| I104 | Tea | 80 |
| i108 | Sugar | 60 |
| I109 | coffee | 100 |

Consider Demand relational database

| ino | Iname | Demand |
|------|--------|--------|
| I105 | Coffee | 80 |
| I107 | Milk | 60 |
| I104 | Tea | 100 |
| I108 | Sugar | 50 |
| I109 | coffee | 80 |

Lossless Join is given by

| Cno | Ino | Iname | price |
|------|------|--------|-------|
| C101 | I105 | coffee | 100 |
| C101 | I107 | Milk | 50 |
| C103 | I104 | tea | 80 |
| C102 | I107 | milk | 80 |
| C101 | I108 | Sugar | 60 |
| C102 | I105 | coffee | 100 |

Lossless decomposition is given by

| ino | Iname | price |
|------|--------|-------|
| I105 | Coffee | 100 |
| I107 | Milk | 50 |
| I104 | Tea | 80 |
| I108 | Sugar | 60 |
| I105 | Coffee | 100 |

| ino | Iname | Demand |
|------|--------|--------|
| I105 | Coffee | 80 |
| I107 | Milk | 60 |
| I104 | Tea | 100 |
| I108 | Sugar | 50 |
| I109 | Coffee | 80 |

3. DATA WAREHOUSING AND DATA MINING

3.1 Data warehousing

The data mining can be performed using data warehousing. In data warehousing information is stored with data or text. The Relational database with data or data as text used to keep the information. For example, super market and new paper business data warehousing [4]

Consider Purchase database

| Cno | Ino | Iname | price |
|------|------|--------|-------|
| C101 | I105 | coffee | 100 |
| C101 | I107 | Milk | 50 |
| C103 | I104 | tea | 80 |
| C102 | I107 | milk | 80 |
| C101 | I108 | Sugar | 60 |
| C102 | I105 | coffee | 100 |

3.2 Data Mining

Data mining is knowledge discovery process dealing with methods like frequent items, association rules, clustering records, representation of tree, classification of trees and uncertainty in data[2,4].

In the following some of the methods are discussed

Customers who purchased more than one Item. Is given by

| Cno | Ino | Iname | price |
|------|------|--------|-------|
| C101 | I105 | coffee | 100 |
| C101 | I107 | Milk | 50 |
| C103 | I104 | tea | 80 |
| C102 | I107 | milk | 80 |
| C101 | I108 | Sugar | 60 |
| C102 | I105 | coffee | 100 |

```
SELECT P.Cno, P.Ino, Iname, COUNT(*)
FROM purchase P
WHERE COUNT(*)>1.
```

| Cno | Ino | COUNT |
|------|------|-------|
| C101 | I105 | 2 |
| C102 | I105 | 2 |

Association rules.

Customers who purchased coffee and milk. is given by

<coffee=><milk>

```
SELECT P.Cno, P.Ino
```

```
FROM purchase P
```

```
WHERE Iname='coffee' and Iname='milk'
```

| Cno | Ino |
|------|------|
| C101 | I105 |
| C102 | I105 |

4. FUZZY DATA MINING

Fuzzy Data Mining is knowledge discovery process with data associated with uncertainty or incompleteness. The fuzzy logic[7, 8] is more suitable to deal with such data because fuzzy logic deals with commonsense rather than likelihood.

Fuzzy Relational Databases are discussed with Rough set theory. Rough Set theory is another approach to incomplete information[16]. The incomplete Information may be deal with fuzzy logic.

Definition: Given some universe of discourse X, a fuzzy rough set is defined as pair $\{t, \mu_d(t)\}$, where d is domains and membership function $\mu_d(x)$ taking values on the unit interval[0,1] i.e. $\mu_d(t) \rightarrow [0,1]$, where $t \in X$ is tuples .

| | d_1 | d_2 | ... | d_n | μ |
|-------|----------|----------|-----|----------|--------------|
| t_1 | a_{11} | a_{12} | - | a_{1n} | $\mu_d(t_1)$ |
| t_2 | a_{21} | a_{22} | - | A_{2n} | $\mu_d(t_2)$ |
| - | - | - | - | - | - |
| t_k | a_{k1} | a_{k2} | - | A_{kn} | $\mu_d(t_k)$ |

Let C and D be the fuzzy rough sets .

The operations on fuzzy rough sets are given as

$$1-C = 1 - \mu_C(x) \quad \text{Negation}$$

$$C \cup D = \max\{\mu_C(x), \mu_D(x)\} \quad \text{Union}$$

$$C \cap D = \min\{\mu_C(x), \mu_D(x)\} \quad \text{Intersection}$$

Consider Price fuzzy database

Fuzzy lossless decomposition is given by

| ino | Iname | price | μ |
|------|--------|-------|-------|
| I105 | Coffee | 100 | 0.8 |
| I107 | Milk | 50 | 0.4 |
| I104 | Tea | 80 | 0.7 |
| I108 | Sugar | 60 | 0.5 |
| I109 | coffee | 100 | 0.8 |

| ino | Iname | Demand | μ |
|------|--------|--------|-------|
| I105 | Coffee | 80 | 0.8 |
| I107 | Milk | 60 | 0.5 |
| I104 | Tea | 100 | 0.8 |
| I108 | Sugar | 50 | 0.5 |
| I109 | Coffee | 80 | 0.8 |

The Negation of Price fuzzy database is given by

| ino | Iname | price | μ |
|------|--------|-------|-------|
| I105 | Coffee | 100 | 0.2 |
| I107 | Milk | 50 | 0.5 |
| I104 | Tea | 80 | 0.8 |
| I108 | Sugar | 60 | 0.5 |
| I109 | coffee | 100 | 0.2 |

| ino | Iname | price | μ |
|------|--------|-------|-------|
| I105 | Coffee | 100 | 0.8 |
| I107 | Milk | 50 | 0.5 |
| I104 | Tea | 80 | 0.8 |
| I108 | Sugar | 60 | 0.5 |
| I105 | Coffee | 100 | 0.8 |

Consider Demand fuzzy relational database

| ino | Iname | Demand | μ |
|------|--------|--------|-------|
| I105 | Coffee | 80 | 0.7 |
| I107 | Milk | 60 | 0.5 |
| I104 | Tea | 100 | 0.8 |
| I108 | Sugar | 50 | 0.4 |
| I109 | coffee | 80 | 0.7 |

For instance fuzzy software database , consider best software Company is given by

| Company | μ |
|-----------|-------|
| IBM | 0.8 |
| Microsoft | 0.9 |
| Novel | 0.6 |
| Oracle | 0.7 |
| Google | 0.75 |

Fuzzy lossless Natural Join of Demand and Price is Union and given as

Rich software company with fuzziness $>.7$ is given by

```
SELECT P.software
FROM software P
WHERE  $\mu > 0.7$ 
```

| ino | Iname | Demand | price | μ |
|------|--------|--------|-------|-------|
| I105 | Coffee | 80 | 100 | 0.8 |
| I107 | Milk | 60 | 50 | 0.5 |
| I104 | Tea | 100 | 80 | 0.8 |
| I108 | Sugar | 50 | 60 | 0.5 |
| I109 | Coffee | 80 | 100 | 0.8 |

| Company | μ |
|-----------|-------|
| IBM | 0.8 |
| Microsoft | 0.9 |
| Google | 0.75 |

Fuzzy intersect of Demand and Price is given by

Consider fuzzy database

| ino | Iname | Demand | price | μ |
|------|--------|--------|-------|-------|
| I105 | Coffee | 80 | 100 | 0.7 |
| I107 | Milk | 60 | 50 | 0.4 |
| I104 | Tea | 100 | 80 | 0.7 |
| I108 | Sugar | 50 | 60 | 0.4 |
| I109 | Coffee | 80 | 100 | 0.7 |

| Cno | Ino | Iname | price | μ |
|------|------|--------|-------|-------|
| C101 | I105 | coffee | 100 | 0.8 |
| C101 | I107 | Milk | 50 | 0.5 |
| C103 | I104 | tea | 80 | 0.8 |
| C102 | I107 | milk | 80 | 0.5 |
| C101 | I108 | Sugar | 60 | 0.8 |
| C102 | I105 | coffee | 100 | 0.8 |

Fuzzy Frequency Items

Customers who purchased more than one Item. Is given by

```
SELECT P.Cno, P.Ino, Iname, COUNT(*)
FROM purchase P
WHERE μ>0.6.
```

| Cno | Ino | COUNT |
|------|------|-------|
| C101 | I105 | 2 |
| C102 | I105 | 2 |

Fuzzy Association rules.

Customers who purchased coffee and milk is given by

```
<coffee=><milk>
SELECT P.Cno, P.Ino
FROM purchase P
WHERE Iname="coffee" and Iname="milk"
and μ>.7
```

| Cno | Ino |
|------|------|
| C101 | I105 |

Fuzzy functional dependency and Association rule

Let R is Relational Database. T is set of tuples. The Functional dependency $FD: X \rightarrow Y$ exists if $t1[X]=t2[X]$ then $t1[Y]=t2[Y]$

A Fuzzy Functional Dependency is defined by $FD: X \rightarrow Y$ exists if $t1[X]$.approximately equal. $t2[X]$ then $t1[Y]$. approximately equal. $t2[Y]$ i.e. if $t1[X].EQ.t2[X]$ then $t1[Y].EQ.t2[Y]$

The fuzzy conditional inference for FFD using Gödel's definition is given by

FFD: $X \rightarrow Y =$
 $1 \quad \mu(t1) \leq \mu(t2)$
 $\mu(t1) \quad \mu(t1) > \mu(t2)$

Consider the fuzzy database

| Cno | Ino | Iname | price | μ |
|------|------|--------|-------|-----|
| C101 | I105 | coffee | 100 | 0.8 |
| C101 | I107 | Milk | 50 | 0.5 |
| C103 | I104 | tea | 80 | 0.8 |
| C102 | I107 | milk | 80 | 0.5 |
| C101 | I108 | Sugar | 60 | 0.8 |
| C102 | I105 | coffee | 100 | 0.8 |

The fuzzy equality Cno is given by

| Cno | EQ |
|---------------|----|
| <C101=><C101> | 1 |
| <C102=><C102> | 1 |
| <C103=><C103> | 1 |

The fuzzy equality Iname given by

| Iname | EQ |
|-----------------|-----|
| <Coffee=><Milk> | 0.8 |
| <Milk=><Coffee> | 0.8 |
| <Tea=><Sugar> | 0.4 |

The FFD: $Cno \rightarrow Iname$ is given by

| Cno | Iname | EQ |
|---------------|-----------------|-----|
| <C101=><C101> | <Coffee=><Milk> | 0.8 |
| <C102=><C102> | <Milk=><Coffee> | 0.8 |
| <C103=><C103> | <Tea=><Sugar> | 0.4 |

The fuzzy association may be given for items with $EQ > 0.5$

| Cno | Iname | EQ |
|---------------|-----------------|-----|
| <C101=><C101> | <Coffee=><Milk> | 0.8 |
| <C102=><C102> | <Milk=><Coffee> | 0.8 |

Find the Items with Price ≥ 0.8

```
SELECT ino
FROM Items
Where Price  $\geq 0.8$ 
```

| ino |
|------|
| I105 |
| I104 |
| I109 |

5. REASONING WITH FUZZY DATA MINING

The Business Intelligence may be studied with Fuzzy data Mining.

Consider the fuzzy conditional inference

If x is A then x is B

Muzimoto fuzzy reasoning is given by [3]

If x is A then x is B

X is more A

X is more B

Provided $\mu_A(x) < \mu_B(x)$

If x is Demand then x is price

X is more demand

X is more Price

From the above tables, more Price is given by

| ino | Price |
|------|-------|
| I105 | 0.89 |
| I107 | 0.71 |
| I104 | 0.84 |
| I108 | 0.71 |
| I109 | 0.89 |

Consider the Iname with fuzzy frequency algorithm.

The fuzzy frequency algorithm is replacing MapReducing algorithm. finding frequency data sets with different fuzzy frequency.

| Cno | Ino | Iname | frequency |
|------|------|--------|-----------|
| C101 | I105 | coffee | 0.75 |
| C101 | I107 | Milk | 0.5 |
| C103 | I104 | tea | 0.7 |
| C102 | I107 | milk | 0.4 |
| C101 | I108 | Sugar | 0.3 |
| C102 | I105 | coffee | 0.0.8 |

item sets for above fuzzy databases is given

| Cno | Ino | Iname | frequency |
|------------|------|--------|-----------|
| C101, C102 | I105 | coffee | 0.75 |
| C101, C102 | I107 | Milk | 0.4 |
| C103 | I104 | tea | 0.7 |
| C101 | I108 | Sugar | 0.3 |

Find the frequency of data sets ≥ 0.6

```
SELECT *
FROM Items
Where frequency  $\geq 0.6$ 
```

| Cno | Ino | Iname | frequency |
|------------|------|--------|-----------|
| C101, C102 | I105 | coffee | 0.75 |
| C103 | I104 | tea | 0.7 |

6. CONCLUSION

Data Mining is Knowledge Discovery Process with data warehousing. The logical and physical data independent is studied by taking examples. The fuzzy reasoning is studied with Fuzzy Data Mining. The advantages of fuzzy Data Mining are minimizing data access costs of Big Data, minimize the multiple copies of functions and objects. Fuzzy databases data sets replace the many MapReducing algorithms. In similar line Xquery may be studied.

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